1. How many different areas of squares can be made by choosing 4 of the 16 dots below as vertices?


Answer: 5

* See the drawings of the squares illustrated below.


2. How many of the following fractions get bigger after 1 is added to the numerator and also to the denominator?

$$
\begin{array}{llll}
\frac{4}{9} & \frac{5}{2} & \frac{3}{2} & \frac{4}{7}
\end{array} \frac{8}{9} \quad \frac{6}{8}
$$

Answer: 4

* They are:

$$
\begin{array}{llll}
\frac{4}{9} & \frac{4}{7} & \frac{8}{9} & \frac{6}{8}
\end{array}
$$

3. The distance that Helen drives in 45 minutes is 3 times the distance that John drives in 30 minutes. If Helen drives at $100 \mathrm{~km} / \mathrm{h}$, how fast does John drive in $\mathrm{km} / \mathrm{h}$ ?

Answer: $50 \mathrm{~km} / \mathrm{h}$

* The distance that Helen drives in 45 minutes is 3 times the distance that John drives in 30 minutes, so Helen drives in 15 minutes to same as John drives in 30 minutes. Then Helen drives in 30 minutes as far as John drives in an hour. John drives $50 \mathrm{~km} / \mathrm{h}$.

4. Various cities and the distances between them are shown on the map below. Using only the paths on the map, what is the shortest distance between A-Town and F-Town? (The diagram is not drawn to scale.)


Answer: 8

* $A \rightarrow D \rightarrow B \rightarrow C \rightarrow F$, the distance is 8 .

5. What is the perimeter of the shape below?


Answer: 28 m

* $2 \times(8+6)=28 m$

6. In the diagram below, we want to shade some circles. What is the maximum number of circles we can shade such that no two shaded circles are connected by a line?


Answer: 4

* See one example illustrated below.


7. In the figure below, what is the angle $x$ ?


Answer: $50^{\circ}$

* $180^{\circ}-32^{\circ}-42^{\circ}-38^{\circ}-18^{\circ}=50^{\circ}$
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8. There are two analog 12-hour watches. One watch runs 3 minutes faster each day, and the other watch runs 2 minutes more slowly each day. If they currently tell the same time, how many days will pass before they tell the same time again?

Answer: 144 days

* Every day, one goes ahead by 5 minutes (relative to the other). They will tell the same time once that watch goes ahead by 12 hours. This will take $12 \times 60$ $\div 5=144$ days.

